

Fundamental Theorem of Algebra

✓ Every n^{th} order Polynomial has exactly ' n ' roots (complex)

Poly:

$$p(x) = a_n x^n + a_{n-1} x^{n-1} + \dots + a_1 x + a_0$$
$$\equiv \sum_{i=0}^n a_i x^i$$

It can be rewritten as

$$p(x) = a_n (x - z_n) (x - z_{n-1}) \dots (x - z_2) (x - z_1)$$
$$\equiv a_n \prod_{i=1}^n (x - z_i)$$

where z_i are polynomial roots can be real or complex.

$$i) \quad x(n) = \delta(n) - a \delta(n-1)$$

→ ROC
ENTIRE
Z PLANE

$$X(z) = \sum_{\forall n} \delta(n) - a \delta(n-1) z^{-n}$$

$$X(z) = 1 - a z^{-1} \quad ; \quad \text{for } |z| \text{ all over not including } 0. \\ \text{i.e., } z=0$$

$$ii) \quad x(n) = a^n u[n]$$

$$X(z) = \sum_{\forall n} a^n u[n] z^{-n}$$

$$= \sum_{n=0}^{\infty} (a z^{-1})^n = \sum_{n=0}^{\infty} (a z^{-1})^n$$

GS

→ ROC
Outside
circle of
radius
|a|

$$X(z) = \frac{1}{1 - a z^{-1}} \quad ; \quad |z| > |a|$$

$$iii) \quad x(n) = -b^n u[-n-1]$$

$$X(z) = \frac{1}{1 - b z^{-1}} \quad ; \quad |z| < |b|$$

→ ROC in
the annular
ring bet
|a| & |b|
radii

$$iv) \quad a^n u(n) - b^n u[-n-1]$$

$$X(z) = \frac{1}{1 - a z^{-1}} + \frac{1}{1 - b z^{-1}}, \quad |a| < |z| < |b|$$